## Oxidation/Reduction Limits for H<sub>2</sub>O

Consider the *Oxidation* of  $H_2O$  to yield  $O_2(g)$ , the half reaction can be written as;

 $2 H_2 O == O_2(g) + 4 H^+ + 4 e^- E^\circ = -1.23 V (from tables)$ 

Re-writing this as a reduction (by convention) and dividing by 4 (for convenience) yields;

$$\frac{1}{4}O_2(g) + H^+ + e^- = = \frac{1}{2}H_2O$$
  $E^\circ = 1.23 V$  (note the sign change in  $E^\circ$ , but the magnitude remains unchanged)

Writing an equilibrium expression for the half reaction yields;

$$K_{eq} = \frac{1}{P_{O2}^{-1/4} \{H^+\} \{e^-\}} = P_{O2}^{-1/4} \{H^+\}^{-1} \{e^-\}^{-1}$$

Isolating  $\{e^-\}^{-1}$  yields;  $\{e^-\}^{-1} = K_{eq} P_{O2}^{1/4} \{H^+\}$ 

and taking log of both sides yields;  $\log \{e^{-}\}^{-1} = \log K_{eq} + \log P_{O2}^{-1/4} + \log \{H^{+}\}$ 

Defining  $pe = -\log \{e^{-}\}$  and  $pH = -\log \{H^{+}\}$  yields;

 $pe = \log K_{eq} + \log P_{O2}^{-1/4} - pH$ 

At the boundary of chemical oxidation of  $H_2O$ , the  $P_{O2} = 1$  atm and so;

$$pe = \log K_{eq} - pH$$
  
Since,  $K_{eq} = 10^{-\frac{\Delta G^{\circ}}{2.3RT}}$ ,  $\log K_{eq} = \frac{-\Delta G^{\circ}}{2.3RT}$  and  $\Delta G^{\circ} = -nFE^{\circ}$ , then  
 $\log K_{eq} = \frac{nFE^{\circ}}{2.3RT}$  and  
 $pe = \frac{nFE^{\circ}}{2.3RT} - pH$ 

In the present case, where n = 1 and  $E^{\circ} = 1.23$  V, the dependence of pe on pH is given by;

pe = 20.8 - pH for the boundary for the oxidation of H<sub>2</sub>O to O<sub>2</sub> where F = 96,485 C/mol, R = 8.314 J/mol K, T = 298 K and 1 CV = J/mol.

When  $H^+$  is at standard state (i.e., 1 M, pH = 0) at 25°C, then

$$pe = pe^{\circ} = \frac{nFE^{\circ}}{2.3RT} = 20.8$$
 (for the oxidation of H<sub>2</sub>O to O<sub>2</sub>)

In general;  $pe^{\circ} = \log K_{eq} = \frac{-\Delta G^{\circ}}{2.3RT} = \frac{E^{\circ}}{0.0591}$ , and  $pe = \frac{E}{0.0591}$  for any one electron process at 25°C.

Consider the *Reduction* of  $H_2O$  to yield  $H_2(g)$ , the half reaction can be written as;

 $2 H_2O + 2 e^- == H_2(g) + 2 OH^- E^\circ = -0.827 V$  (from tables)

Re-writing this reduction dividing by 2 (for convenience) yields;

 $1/2 H_2O + e^- == \frac{1}{2} H_2(g) + OH^- E^\circ = -0.827 V$ (note the magnitude of  $E^\circ$  remains unchanged)

Writing an equilibrium expression for the half reaction yields;

$$K_{eq} = P_{H2}^{1/2} \{OH^{-}\} \{e^{-}\}^{-1}$$

Isolating  $\{e^{-}\}^{-1}$  and taking log of both sides yields;

$$\log \{e^{-}\}^{-1} = \log K_{eq} + \log P_{H2}^{-1/2} + \log \{OH^{-}\}^{-1}$$

Defining  $pe = -\log \{e^-\}$  and  $pOH = -\log \{OH^-\}$  yields;

 $pe = \log K_{eq} + \log P_{O2}^{-1/2} + pOH$ 

At the boundary of chemical reduction of  $H_2O$ , the  $P_{H2} = 1$  atm and so;

 $pe = \log K_{eq} + pOH$ 

Since  $pK_w = pOH + pH$ , we can substitute  $pOH = pK_w - pH$  thus;

 $pe = \log K_{eq} + pK_w - pH$ 

As before,

$$\log K_{eq} = \frac{nFE^{\circ}}{2.3RT} \text{ and}$$
$$pe = \frac{nFE^{\circ}}{2.3RT} + pK_{w} - pH$$

In the present case, where n = 1,  $E^{o} = -0.827$  V and  $pK_{w} = 14$ , the dependence of pe on pH is given by;

 $pe = \frac{(1)(96485)(-0.827)}{2.3(8.314)(298)} + 14 - pH = -pH \text{ (note that the units in nFE}^{\circ}/2.3RT \text{ cancel)}$ 

When H<sup>+</sup> is at standard state (i.e., 1 M, pH = 0) at 25°, then  $pe = pe^{\circ} = 0$  for the reduction of H<sub>2</sub>O to H<sub>2</sub>.

At other  $\{H^+\}$ , the boundary between  $H_2O$  and  $H_2$  is given by; pe = -pH